

The role of magnetic forces in biology and medicine

Bradley J Roth

Department of Physics, Oakland University, Rochester, MI 48309, USA
Corresponding author: Bradley J Roth. Email: roth@oakland.edu

Abstract

The Lorentz force (the force acting on currents in a magnetic field) plays an increasingly larger role in techniques to image current and conductivity. This review will summarize several applications involving the Lorentz force, including (1) magneto-acoustic imaging of current; (2) 'Hall effect' imaging; (3) ultrasonically-induced Lorentz force imaging of conductivity; (4) magneto-acoustic tomography with magnetic induction; and (5) Lorentz force imaging of action currents using magnetic resonance imaging.

Keywords: Lorentz force, magnetic field, ultrasound, magnetic resonance imaging, conductivity, magneto-acoustic imaging

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Introduction

Over the last 20 years, several research groups have developed imaging methods that take advantage of the force acting on biocurrents when a magnetic field is present. The underlying mechanism is familiar to anyone who has taken an introductory physics class:¹ a wire carrying a current I , having a length L and lying perpendicular to a magnetic field B experiences a magnetic force $F = ILB$, often called the 'Lorentz force.' The direction of the force is at right angles to both the wire and the magnetic field, and can be determined by a 'right-hand-rule.' This is the same force that makes electric motors work.

As the Lorentz force results from a magnetic field and produces mechanical motion, phenomena that arise from it are often referred to as 'magneto-acoustics.' In biological tissue, where wires are not present, it is more convenient to speak of the Lorentz force per unit volume, F , arising from the current density J and the magnetic field B : $F = J \times B$, where ' $\times$ ' indicates the cross product (Figure 1). In general, magneto-acoustic effects are small, but small effects underlie many important imaging techniques.

In this minireview, I will discuss biological and medical applications of magneto-acoustics. These techniques could be useful for mapping electrical activity in the brain and heart, and for detecting abnormal tissues – such as tumors – by changes in electrical properties. I focus on magnetic forces that act on electric current, with an emphasis on how these forces can be used to image current or conductivity. Topics I will not address include: safety issues arising from strong magnetic fields,^{2–4} effects arising from the presence of iron that result in particularly large magnetic forces (e.g. magnetite particles in magnetotactic bacteria⁵),

and phenomena related to electron or nuclear spin (such as nuclear magnetic resonance).

Magneto-acoustic imaging of current

In 1988, Bruce Towe and his colleagues^{6,7} developed a 'novel method for the noninvasive measurement of low-level ionically conducted electric currents flowing in electrolytes and tissues.' They pass AC current (3 kHz) with a strength of a few microamperes through a hamster placed in a 0.2 T magnetic field (Figure 2). The acoustic signal arising from the Lorentz force is detected using a microphone and a lock-in amplifier. They conclude⁶ 'these experiments show that it is possible to noninvasively detect the existence of ionic currents flowing interior to a conducting medium by applying magnetic fields and monitoring the resulting acoustic responses. This principle is of interest as a possible basis for a new method of noninvasively measuring bioelectric currents in living organisms.' Later, Towe⁸ further developed an instrument that 'is basically a very sensitive force-balance that can measure Lorentz forces experienced by ionic currents flowing in small objects when exposed to strong oscillating magnetic fields.' Although this method has not yet become widely used to image current, it demonstrates the feasibility of measuring magneto-acoustic effects and illustrates the physical principles at work.

Towe's technique can detect applied AC currents of a known frequency, but can it be used to detect endogenous action currents in nerve and muscle? To answer this question, Roth *et al.*⁹ analyzed magneto-acoustic phenomena theoretically. They calculate the pressure p and

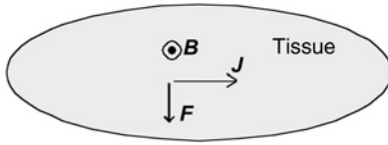


Figure 1 The Lorentz force. Current density J flows to the right, and the magnetic field B is directed out of the paper (indicated by the symbol $\odot$), resulting in a force F downward

displacement u produced by a current density J in an elastic conducting tissue having a shear modulus G and exposed to a magnetic field B , starting from Navier's equation,

$$G\nabla^2 u - \nabla p + J \times B = 0. \quad (1)$$

This equation is motivated by the fluid-fiber-collagen model of cardiac tissue,¹⁰ in which the pressure is caused by the fluid (assumed to be incompressible, $\nabla \cdot u = 0$) and the shear modulus arises from the elastic properties of collagen fibers. Equation 1 relates the forces that arise by elastic shearing, by pressure gradients and by the Lorentz force. The divergence of (Eq. 1) shows that the source of the pressure is the curl of the current density

$$\nabla^2 p = (\nabla \times J) \cdot B. \quad (2)$$

This result reveals an analogy between magneto-acoustic current imaging and biomagnetic current imaging.⁹ The curl of Ampere's law, $\nabla \times b = \mu_0 J$, governing the biomagnetic field b produced by action currents J , yields

$$\nabla^2 b = -\mu_0 \nabla \times J, \quad (3)$$

where μ_0 is the permeability of free space. Magneto-acoustic pressure recordings (Eq. 2) and biomagnetic measurements

(Eq. 3) image action currents in an equivalent way: they both have $\nabla \times J$ as their source term.

Roth *et al.*⁹ obtain analytical solutions for the displacement produced by a current dipole of strength q at the center of a conducting sphere of radius a . The magnitude of the displacement at the sphere surface is on the order of $qB/(4\pi Ga)$. For a dipole of strength $q = 1 \mu A m$, a shear modulus of $G = 10^4 N/m^2$, a magnetic field of $B = 1 T$ and a radius of $a = 1 cm$, the surface displacement is very small, on the order of 1 nm. Their analysis indicates that 'magneto-acoustic imaging of endogenous bioelectric currents might be significantly more difficult to achieve than might be inferred from the experiments reported to date.'

Ammari *et al.*¹¹ have examined localization methods for magneto-acoustic current imaging mathematically. Their approach is to average measurements of the pressure weighted by particular solutions of the wave equation, which allows them to locate dipole sources. This method can be extended to the case when the pressure is measured over only part of the tissue boundary.

'Hall effect' imaging

Han Wen¹²⁻¹⁴ and his co-workers developed a method of imaging the electrical properties of a sample using what they call the 'classical Hall effect' (Figure 3). Their signal is produced by¹² 'the charge separation phenomenon in a conductive object moving in a magnetic field. This charge separation is a result of the opposing Lorentz forces on the positive and negative charges, and leads to an externally detectable voltage. ...[The] voltage amplitude is determined by the strength of the Lorentz force and the charge density and mobility.' They test their method by applying an ultrasound signal (1 MHz) to a saline chamber containing a sample (a polycarbonate block) that is placed in a 4 T static magnetic field. The sample motion is caused by the

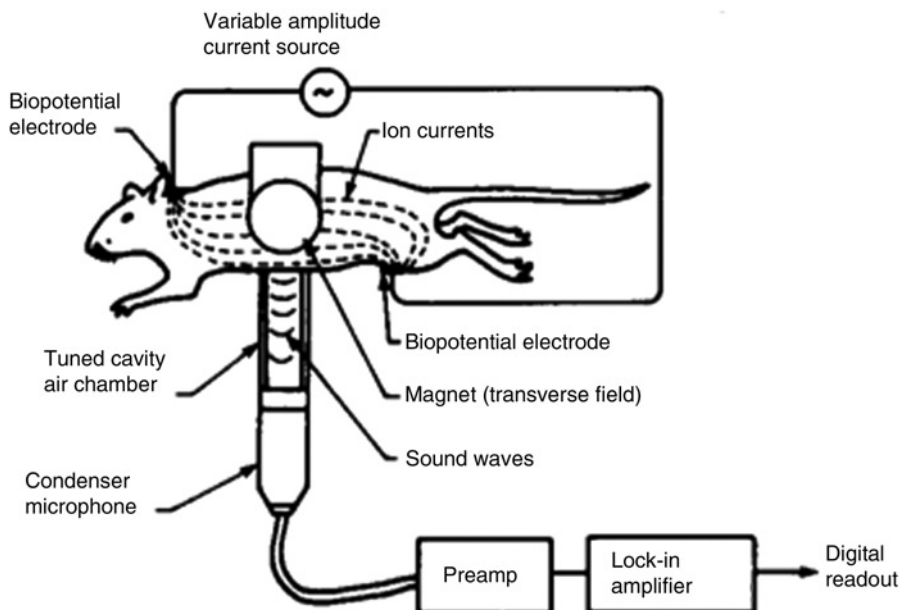


Figure 2 An experiment for the magneto-acoustic detection of current in a hamster. From Towe and Islam.⁶ (© 1988 IEEE)

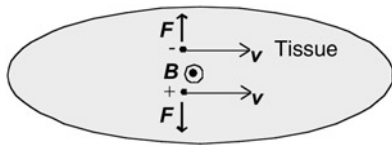


Figure 3 A motion-induced voltage. Tissue is moving with speed v to the right in the presence of a magnetic field B directed out of the paper. Negative ions experience an upward Lorentz force, and positive ions experience a downward Lorentz force. The resulting charge separation produces a negative voltage at the top of the tissue and a positive voltage at the bottom

ultrasonic wave. They measure the induced voltage with electrodes, and are able to obtain clear signals corresponding to the upper and lower surfaces of the sample. Roth and Wikswo¹⁵ have questioned whether the 'Hall effect' is the correct name of the physical mechanism underlying this phenomenon, but in any case the technique represents a novel and important application of Lorentz forces to biomedical imaging.

A reverse 'Hall effect' imaging technique is possible, with the current driven by a voltage source and the motion produced by the Lorentz force (like in magneto-acoustic imaging). Wen *et al.*¹² write that 'in the reverse mode, or ultrasound detection mode, the pulser that was used to drive the ultrasound transducer is now connected to the pair of electrodes that were used to detect the... voltage in the forward mode, and the signal-sensing electronics are connected to the transducer. When the pulser generates a voltage pulse across the electrodes, [it produces] a current density proportional to the local apparent conductivity. At interfaces of changing conductivity the current density becomes discontinuous, and so are the Lorentz forces on the currents...[resulting] in ultrasound pulses emanating from these interfaces.' They use this method to obtain images of the fat-muscle layers in bacon (Figure 4). Roth and Wikswo¹⁵ analyze this reverse method, and derive a wave equation for the ultrasonic pressure signal similar to (Eq. 2) above

$$\nabla^2 p - \frac{1}{c^2} \frac{\partial^2 p}{\partial t^2} = (\nabla \times J) \cdot B, \quad (4)$$

where c is the speed of sound in the tissue. They conclude that¹⁵ 'much of what we learned from a quasistatic analysis of magneto-acoustic imaging can be applied [to] the second [reverse] imaging method proposed by Wen *et al.*'

Ultrasonically-induced Lorentz force to image conductivity

Inspired by Wen *et al.*'s method, Amalric Montalibet and his co-workers^{16,17} further developed 'ultrasonically-induced Lorentz force' methods to measure electrical conductivity (Figure 5). The gist of their technique is the same as described by Wen *et al.*: 'the ions of solutions exposed to the propagation of ultrasound in the presence of a magnetic field experience Lorentz force. Their movement gives rise to a local electric current density, which is proportional to the electric conductivity of the medium... The magnitude of the

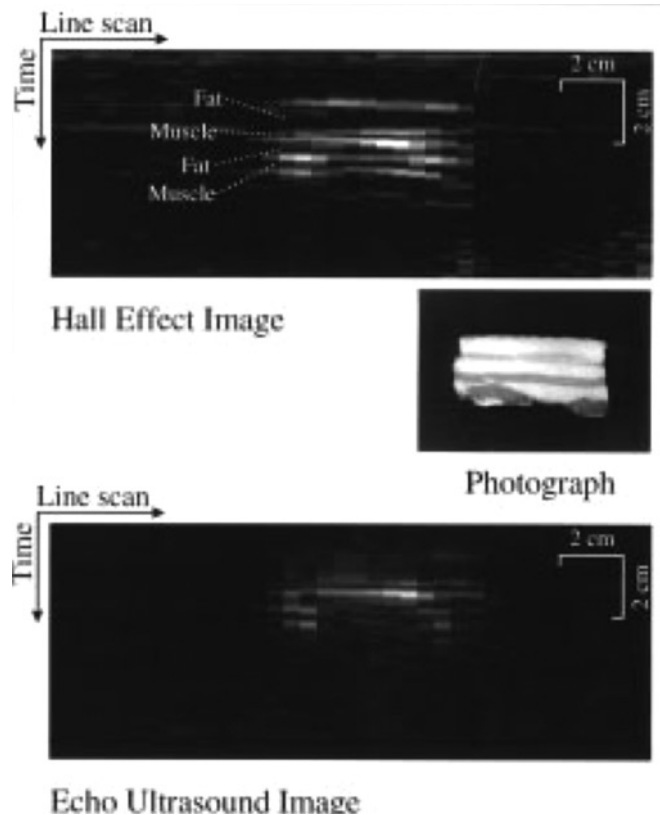


Figure 4 A photograph of the cross-section of a block of bacon, an image of the bacon collected with the reverse-mode Hall effect imaging technique, and an echo ultrasound image of the same cross section. From Wen *et al.*¹² (© 1998 IEEE)

measured current is 50 nA in a saline solution of 0.5 S/m conductivity. The technique enabled the determination of the conductivity of porcine blood sample against haematocrit.¹⁷

Whereas Montalibet *et al.*^{16,17} applied pulsed ultrasound in their experiments, Roth and Schalte¹⁸ derived a tomographic method to obtain the tissue conductivity using continuous-wave ultrasound. The strength and timing of the electric dipole caused by the ultrasonically-induced Lorentz force determines the amplitude and phase of the Fourier transform of the conductivity image. Electrical measurements at a variety of wavelengths and directions are therefore equivalent to mapping the Fourier transform of the conductivity distribution in spatial frequency space. An image of the conductivity itself is then found by taking the inverse Fourier transform. In an alternative approach, Haider *et al.*¹⁹ have examined this problem from the point of view of lead fields. Interestingly, Olafsson *et al.*²⁰ have shown that an ultrasonic wave can itself modify the conductivity, and this effect may need to be taken into account during conductivity imaging.

Tseng and Roth²¹ described a novel feature of the ultrasonically-induced Lorentz force in anisotropic tissue: an oscillating electrical potential propagates along with the ultrasonic wave. This potential is analogous to ultrasonic vibration potentials arising from differences in inertia between positive and negative charge carriers in colloidal suspensions or ionic solutions,²² but it is caused by a

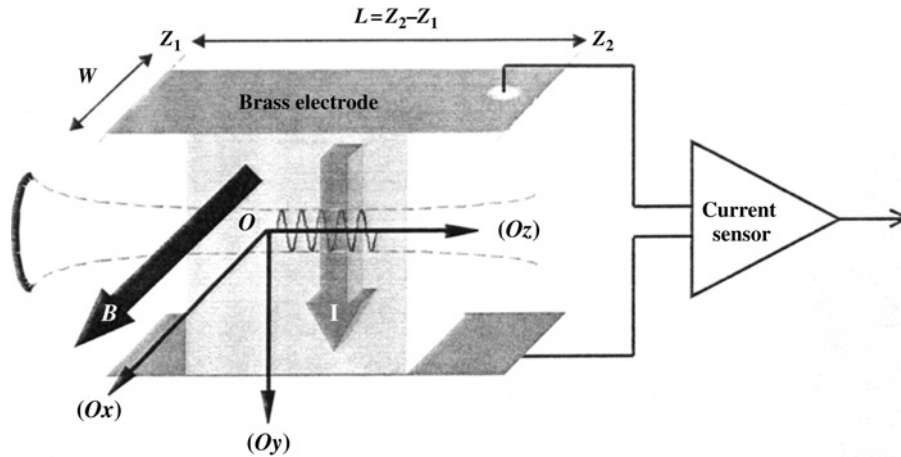


Figure 5 Schematic diagram of the experimental setup for detection of currents caused by the ultrasonically-induced Lorentz force. Axis Oz is the ultrasound propagation axis, Ox has the same orientation as the magnetic field, and the interaction current is positive along Oy . The origin, O , is located at the focal point of the transducer. From Montalibet *et al.*¹⁶

different mechanism. Figure 6 shows three half-wavelengths of an ultrasonic wave that is propagating to the right in a magnetic field coming out of the paper. The current density because of the Lorentz force tilts away from the z -direction owing to the anisotropy (the diagonal lines indicate the fiber direction). This causes positive charge to accumulate where the current vectors converge, and negative charge where they diverge. The charge produces its own electric current and potential that oscillates with the ultrasonic wave.

Magneto-acoustic tomography with magnetic induction

Recently, Bin He and his colleagues have developed magneto-acoustic methods for measuring impedance.^{23–31} The novel feature of their method is that they induce eddy

currents in the sample using magnetic induction (Faraday's law: a changing magnetic field induces an electric field): 'The sample is located in a static magnetic field and a time-varying magnetic field. The time-varying magnetic field induces an eddy current in the sample. Consequently, the sample will emit ultrasonic waves by the Lorentz force. The ultrasonic signals are collected around the object to reconstruct images related to the electrical impedance distribution in the sample.'²³ Li *et al.*²⁵ obtained conductivity boundary images with high spatial resolution from saline and gel phantoms (Figure 7), indicating the feasibility of their method, which they call Magneto-Acoustic Tomography with Magnetic Induction (MAT-MI). Brinker and Roth³² analyzed MAT-MI and found that when imaging nerve or muscle, electrical anisotropy can have a significant effect on the acoustic signal and must be accounted for in order to obtain accurate images. Ammari *et al.*¹¹ have examined MAT-MI reconstruction methods mathematically.

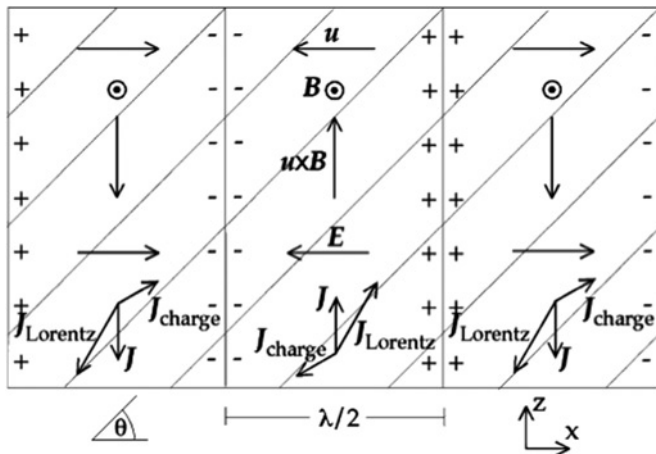


Figure 6 Three half wavelengths of an ultrasonic wave propagating to the right. The magnetic field, B , is coming out of the paper, and the displacement, u , is along the x -axis. The current density caused by the Lorentz force, J_{Lorentz} , is rotated by the tissue anisotropy (fiber axis indicated by diagonal lines), producing a current density and electrical potential caused by charge, J_{charge} . From Tseng and Roth²¹

Lorentz force imaging of action currents using MRI

Allen Song and his co-workers^{33–35} have proposed a method for MRI detection of biocurrents, called 'Lorentz effect imaging.' When exposed to a magnetic field, current in the body is subject to the Lorentz force (Figure 1). This force deforms the tissue, causing the current-carrying nerve fibers to move. When a magnetic field gradient is present, this movement displaces the nerve into a region of different magnetic field strength. If the change in magnetic field is large enough, it causes an artifact in a magnetic resonance signal that can be used to locate the active neurons. Song and Takahashi³³ demonstrate this method by imaging the movement of a copper wire in a gel phantom using MRI. More recently, Truong and Song³⁵ applied 'a series of oscillating gradients (with positive and negative lobes of the same amplitude and duration) in synchrony with the neural stimulation, such that the

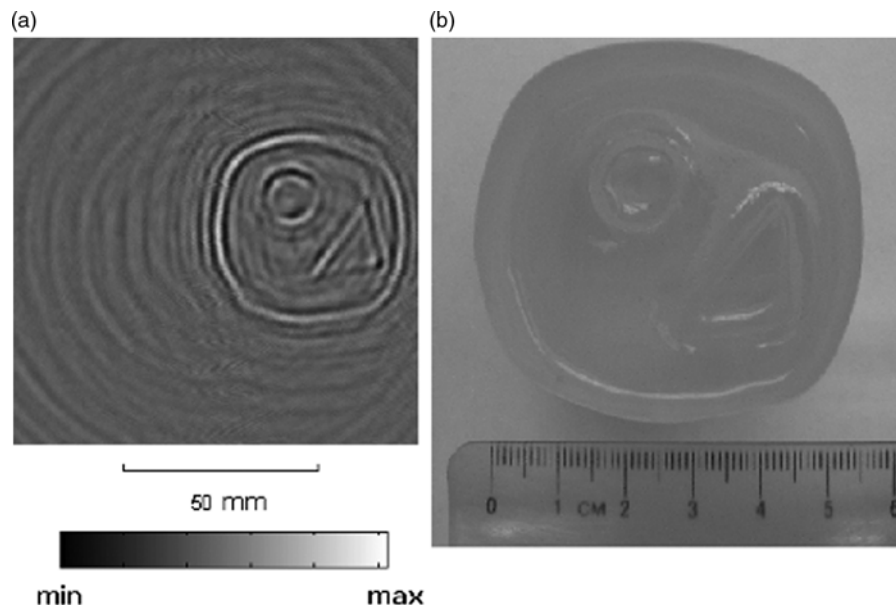


Figure 7 (a) The two-dimensional MAT-MI image of a gel phantom, with two columns of 0% salinity gel embedded in gel of 10% salinity. (b) Top view photo of the phantom. From Li *et al.*²⁵ (© 2007 IEEE)

neuroelectric activity occurs only during the negative lobes.' They conclude that 'the successful detection of neuroelectric activity *in vivo* by using our technique demonstrates that neural activation can be imaged noninvasively by MRI with a high spatial and temporal resolution.' Basford *et al.*³⁶ have also examined Lorentz-force-induced motion during magnetic resonance imaging.

Roth and Bassar³⁷ have analyzed Lorentz force MRI, and predict that the peak displacement u of a nerve of radius a in an arm of radius b is

$$u = \frac{BJ}{4G} a^2 \ln\left(\frac{b}{a}\right), \quad (5)$$

where B is the magnetic field, J is the current density and G is the shear modulus. Using realistic parameters for a human medial nerve in a 4 T field, they calculate a maximum displacement of 13 nm or less, and find a displacement distribution that is not localized around the nerve (Figure 8). They suggest that this displacement is too small and diffuse to be detected by MRI methods. In fact, the biomagnetic fields produced by action currents should result in a larger artifact in the MRI than that caused by the Lorentz effect,³⁸ and whether such biomagnetic fields can be used with MRI to image action currents remains an open question.³⁹ Analysis of the Lorentz effect on ions in solution is similarly controversial,^{40,41} and magnetohydrodynamic effects may be important in this case.⁴²

Conclusion

The Lorentz force is a new tool for obtaining images of current and conductivity in tissue. In general, these forces and the resulting displacements are small. The most promising results to date result from working at high frequencies, where the oscillating force gives rise to ultrasonic waves that

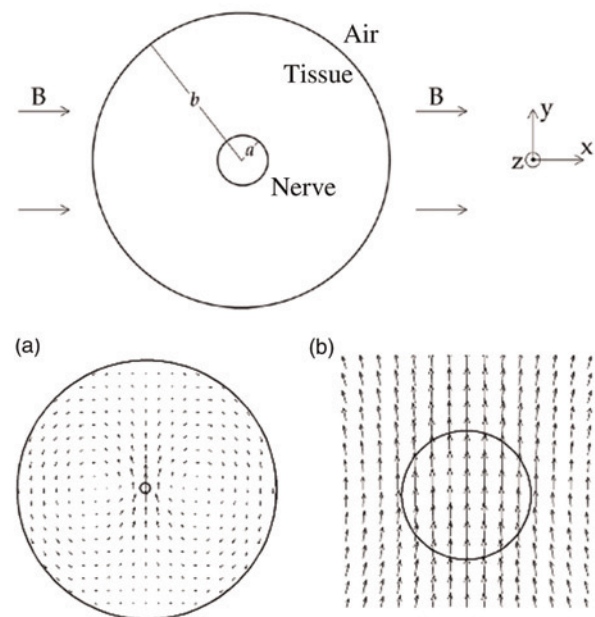


Figure 8 Top: A nerve of radius a lying in an arm of radius b . The magnetic field is in the x direction. Current inside the nerve flows in the positive z direction (out of the page) and the current in the surrounding tissue flows in the negative z direction. Bottom: The displacement caused by the Lorentz force. (a) The entire arm and (b) a detailed view of the displacement around the nerve. The length of the displacement arrows are exaggerated for easy viewing. From Roth and Bassar³⁷

can be detected even if the underlying displacement is very small. Conductivity imaging can be performed in two ways: using an oscillating Lorentz force to generate ultrasound images (Figure 1), or applying ultrasound and detecting the resulting electrical signal (Figure 3). It is not yet clear which of these methods will be most useful in biomedical imaging. Lorentz force methods to measure current have interesting analogies to biomagnetic methods, and share

many of the same strengths and weaknesses. These methods generally require strong magnetic fields, which may be difficult and expensive to produce. They do, however, take advantage of and combine many of the strengths of both bioelectric and biomagnetic techniques with well-established ultrasonic imaging methods. Magneto-acoustic techniques to measure current would compete with established methods such as the electrocardiogram, the magneto-cardiogram, the electroencephalogram and the magnetoencephalogram. Methods to measure conductivity would provide similar information as electrical impedance imaging.

In summary, a growing number of imaging techniques are based on the Lorentz force, and these methods provide great promise for obtaining images of current and conductivity.

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